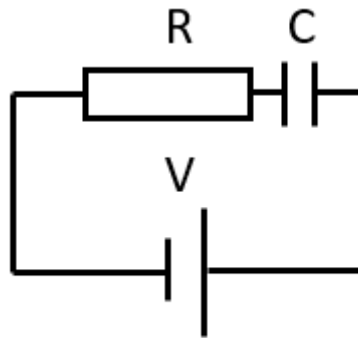


Lesson 7

Resistor Capacitor and Resistor Inductor Circuits

If a resistor and capacitor are connected in series, the capacitor charges gradually through the resistor until the voltage across the resistor is equal to the supply voltage.



Series RC circuit

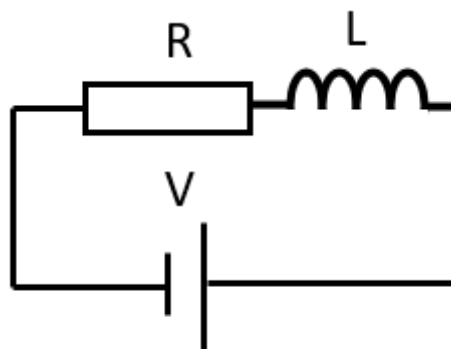
Figure 1

The time, in seconds, for the capacitor to charge depends on the resistor in Ohms and capacitor in Farads.

$$T = C \times R$$

Example: 1 MΩ resistor, 6 uF capacitor with a V of 12 V,

$$T = R \times C = 1 \times 6 = 6 \text{ seconds.}$$



Series RL circuit

Figure 2

If a resistor and inductor are connected in series, the self-inductance of the coil will resist the current flow as the magnetic field is generated. Once the field reaches its peak only the resistor will limit current flow. The time for the field to generate can be calculated.

Time in seconds, resistance in Ohms and inductance in Henries.

$$T = \frac{L}{R}$$

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Example: 1kΩ resistor, 14 mH inductor and V of 12 V.

$$T = L / R = 14 / 1 = 14 \text{ seconds.}$$

Resonance

The useful thing about LC circuits is that with any combination of the C value and the L value, they will have a resonant frequency. At this resonant frequency, the circuits act differently than the components individually.

A parallel LC circuit, Figure 3, will block any signal that is operating on the resonant frequency. In a parallel LC circuit at resonance, the time taken for the capacitor to charge and discharge, is the same time taken for the inductor to charge and discharge.

The energy in the circuit will charge the capacitor and, as the capacitor discharges, the energy will charge the inductor. As the inductor discharges, the energy recharges the capacitor. So, at the resonant frequency, the parallel LC circuit will oscillate.

The combined reactance is high increasing the impedance. So, at resonance, the parallel tuned circuit has a high impedance to the alternating signal.

A signal at any other frequency will pass through the parallel LC circuit.

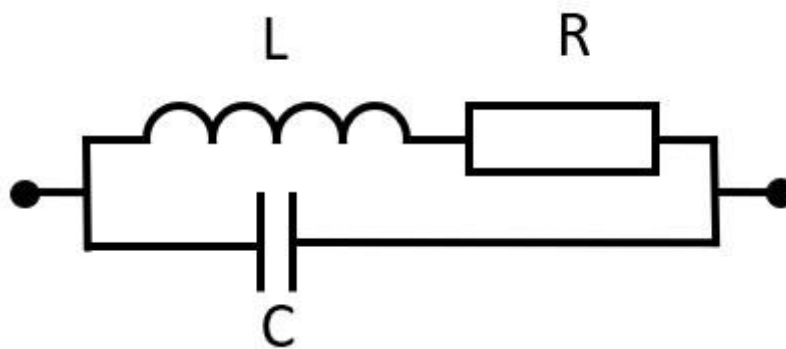


Figure 3 Parallel Circuit

In a series LC circuit, Figure 4, the energy goes through one component then the next. Any signal below the resonant frequency will be blocked by the capacitor. Signals above the resonant frequency will be blocked by the inductor. Signals at the resonant frequency are not blocked by the capacitor or the inductor.

At resonance in the series tuned circuit, the reactance cancels each other leaving only resistance in the circuit. So, at resonance, this circuit has a low impedance to the alternating signal.



Figure 4 Series Circuit

These LC circuits are an essential building block in communications equipment. They can act as filters, tuning circuit for a radio, or the basis of an oscillator.

Impedance and Reactance

Reactance resists current without dissipating power, unlike resistors. Inductive reactance increases with frequency and inductance. Capacitive reactance decreases with frequency and capacitance. Impedance represents total opposition provided by reactance and resistance. See Figure 5.

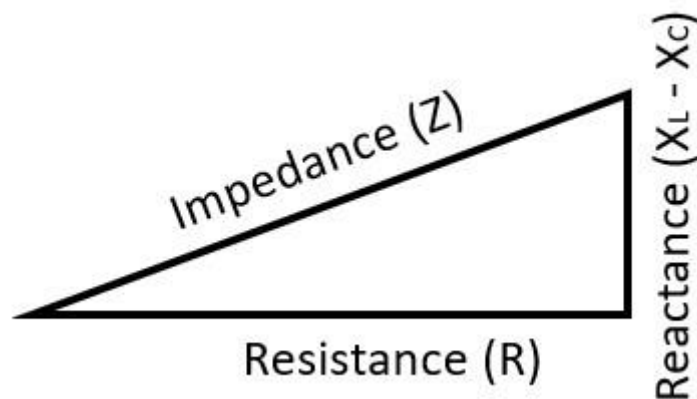


Figure 5

The reactance of a capacitor or inductor can be calculated depending on the frequency.

Inductor reactance

$$X_L = 2 \times \pi \times f \times L$$

X_L = Inductor reactance in Ohms

f = frequency in hertz (Hz)

L = Inductance in Henries

π = 3.141

Example: Inductive reactance of 1H inductor at 30 MHz. (Choke)

$$\begin{aligned} X_L &= 2 \times 3.141 \times 30000000 \times 1 \\ &= 188 \text{ M}\Omega \end{aligned}$$

Capacitive Reactance

$$X_C = \frac{1}{2\pi f C}$$

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X_C = Capacitive reactance in Ohms

f = frequency in hertz (Hz)

C = capacitance in Farads

π = 3.141

Example: Capacitive reactance of 0.01 uF capacitor at 30 MHz. (A HF bypass capacitor)

$$\begin{aligned}X_L &= 1 / (2 \times 3.141 \times 30000000 \times 0.0000001) \\ &= 18.8 \Omega\end{aligned}$$

Frequency

$$f = \frac{1}{2 \times \pi \sqrt{L \times C}}$$

f = frequency in hertz (Hz)

C = capacitance in Farads (F)

L = inductance in Henries (L)

π = 3.141

Example: What is the resonant frequency of a capacitor of 1 uF and an inductor of 1 uH

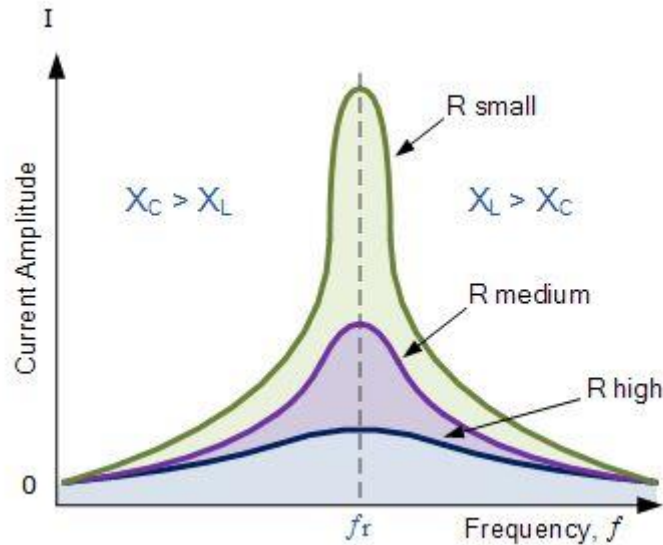
$$\begin{aligned}f &= 1 / (2 \times \pi \sqrt{0.000001 \times 0.000001}) \\ &= 1 / 6.282 \times 0.00141 \\ &112.5 \text{ Hz}\end{aligned}$$

Q Factor

The ratio of the reactance to the resistance, in an operational circuit, is called the Q (Quality Factor) of the circuit. If the current in the circuit is plotted against frequency, either side of the resonant frequency, the result will be a Q plot resembling a bell curve. The base of the bell and the height of the bell indicate the bandwidth of the circuit.

A sample Q plot of a series tuned circuit is shown in Figure 6. As the frequency drops, the capacitive reactance X_C is predominant while the inductive reactance X_L is predominant in the higher frequencies.

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Series Circuit

$$Q = X / R_s \quad \text{or} \quad Q = (2 \times \pi \times f \times L) / R_s$$

Q = Quality factor

X = reactance of capacitor or inductor

R_s = series resistance in Ohms.

Example Series circuit X_L and X_C 350 Ω and a resistance of 10 Ω

$$Q = X / r = 350 / 10 = 35$$

Parallel Circuit

Were R, L and C are in parallel, the lower the parallel resistance, the more effect it will have in damping the circuit and lower the Q. This is useful in filter design to determine the bandwidth.

$$Q = R_p / X \quad \text{or} \quad Q = R_p / (2 \times \pi \times f \times L)$$

Q = Quality factor

X = reactance of capacitor or inductor

R_p = parallel resistance in Ohms.

Example Parallel circuit X_L and X_C 350 Ω and a resistance of 10 Ω

$$Q = R_p / X = 10 / 350 = 0.02$$

Bandwidth

The bandwidth is directly related to the frequency and Q of the circuit.

$$BW = f / Q$$

BW = hertz (Hz)

F = hertz (Hz)

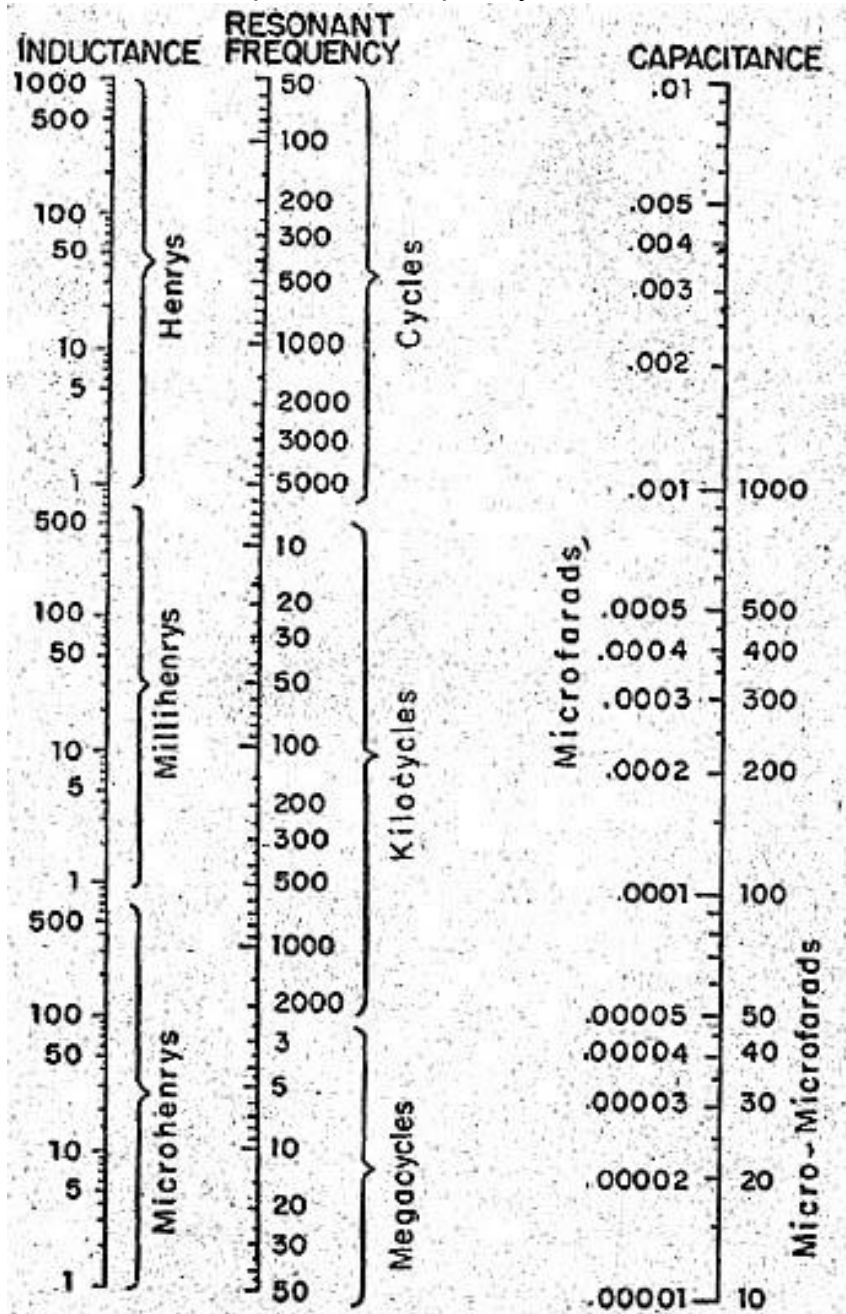
Q = quality factor.

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Example: What is the bandwidth of a 14 MHz circuit with a Q of 35?

$$BW = F / Q = 14000000 / 35 = 400,000 \text{ Hz}$$

I found the following table in Coyne's Television and Radio Handbook P183. This gives a good starting point to match L and C for a particular frequency.



Filters

Electronic filters remove unwanted frequency components from the applied signal, enhance wanted ones or both.

Filters fall into four basic categories as shown below.

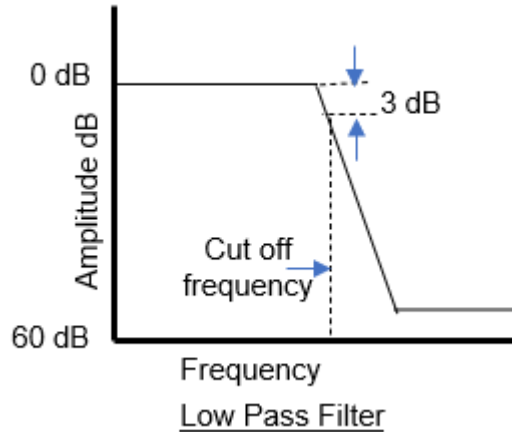
Filters can be constructed with active and or passive components. Only passive components will be used in the following examples.

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The cut off frequency is usually selected as the frequency where the filter loss is -3dB. The -3dB point is also known as the "half power" point.

Low-pass filters

A low-pass filter (LPF) only passes signals below its cutoff frequency while attenuating all signals above.



Choke

A choke is a simple low pass filter. The inductor will pass signals until the Inductive reactance rises high enough to block the signals.



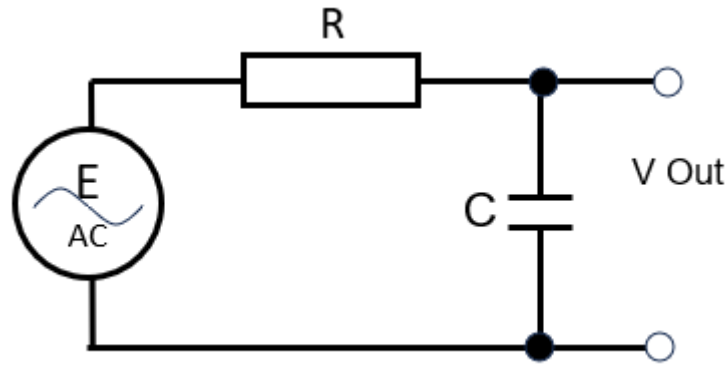
Example: What frequency would a 100mH choke reach 1 k Ω cut off?

$$X_L = 2 \times \pi \times f \times L$$

$$f = X_L / 2\pi L = 1000 / (6.282 \times 0.100) = 1000 / 0.62 = 1612 \text{ Hz}$$

RC Filter

The RC low pass filter will allow low frequency signals to pass until the capacitive reactance becomes low enough to pass signals.

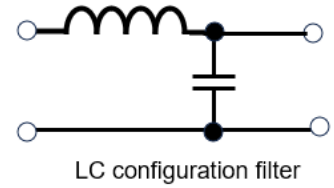
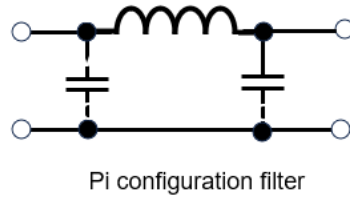
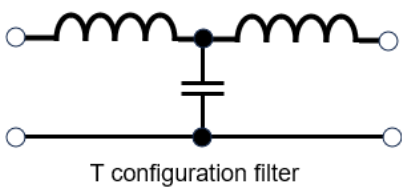


Example: What size capacitor is needed to prevent signals above 1MHz passing to V Out (XL = 10 Ohms)?

$$X_C = \frac{1}{2\pi f C}$$

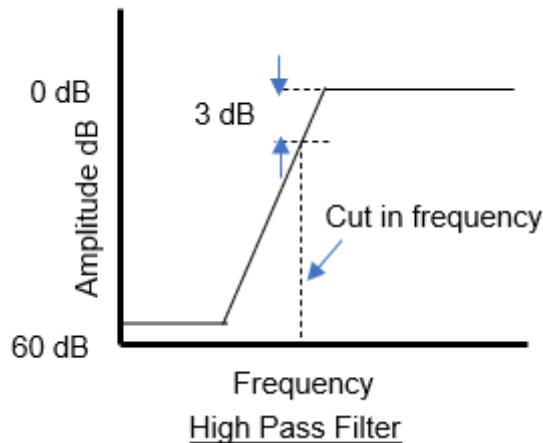
$$C = 1 / (2\pi f X_L) = 1 / 6.282 \times 1000000 \times 10 = 1\text{nF Capacitor}$$

LC Low Pass Circuits

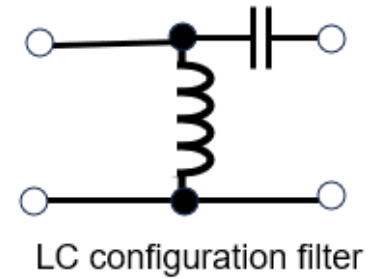
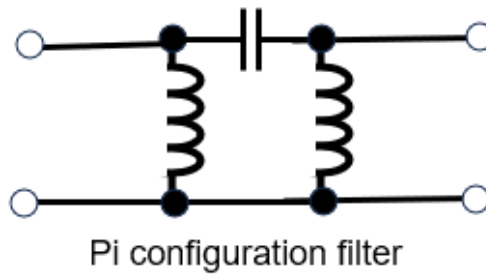
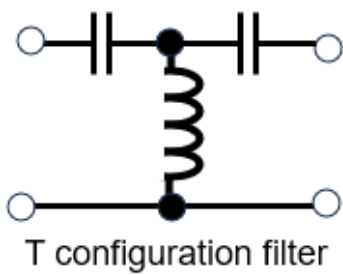


High-pass filters

A high-pass filter (HPF) only passes signals above its cutoff frequency and attenuates all signals below.

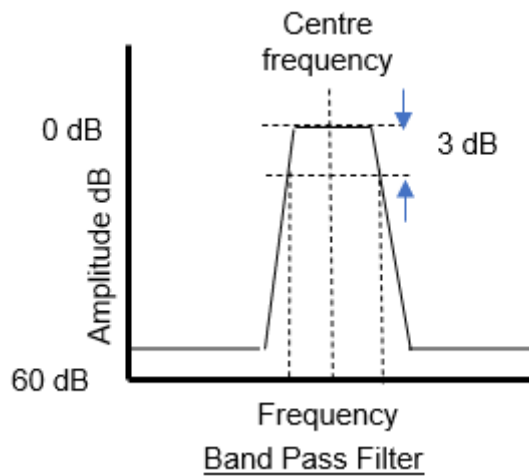


LC High Pass Circuits



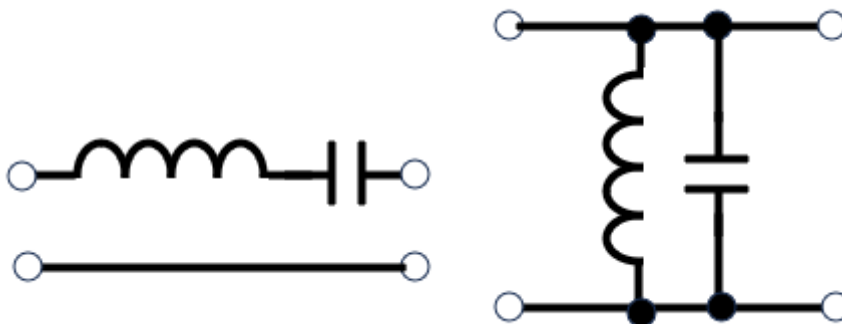
Band-pass filters

A band pass filter (BPF) allows signals within a selected range of frequencies to pass and any frequencies outside this band are attenuated.



Configurations

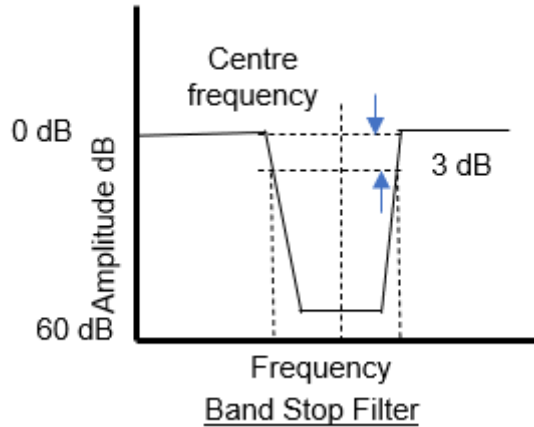
The series LC circuit will only allow the resonant frequency to pass through. The parallel LC circuit will allow all frequencies, except the resonant frequencies to pass to earth.



Band-stop filters

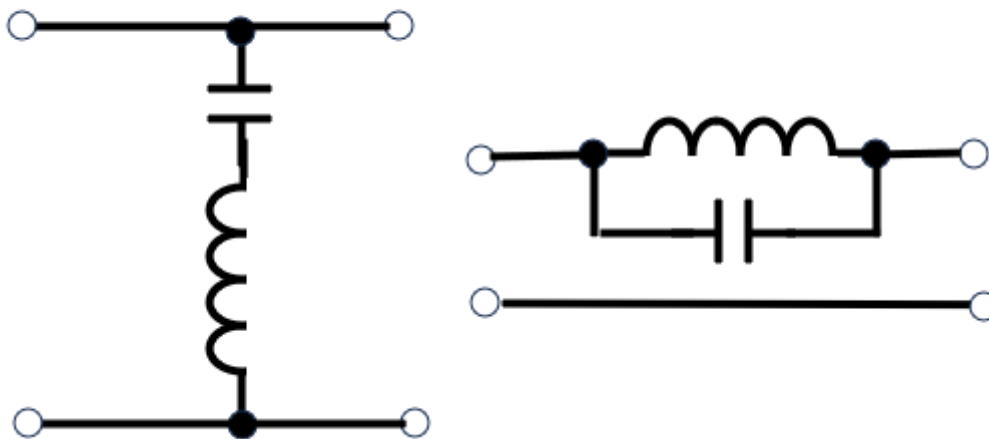
A band stop filter (BSF) attenuates signals within a selected range of frequencies and allows the frequencies outside this band to pass.

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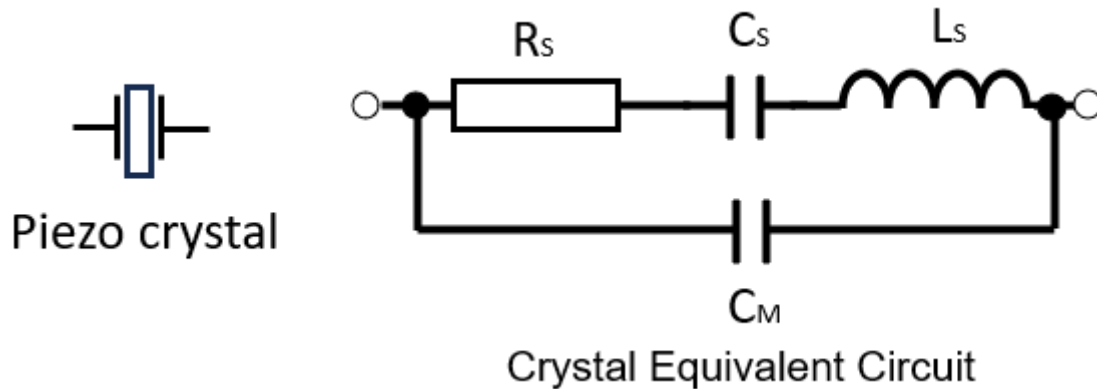
Configurations

The series LC circuit will pass the resonant frequency to earth and block that from going through. The parallel LC circuit will block the resonant frequency from passing.



Quartz crystal Filters

A crystal is a piezoelectric device that uses mechanical resonance to achieve a very precise frequency output. The most common type of crystal material is quartz, but different piezoelectric materials may be used.



The above equivalent circuit consists of a series R_s - C_s - L_s circuit in parallel with a capacitance C_m . When the crystal mounted across the AC source is not vibrating, it is equivalent to the capacitance C_m . However, when the crystal vibrates, it acts like a tuned series R-L-C circuit.

Variations

Butterworth Filter

The Butterworth filter is an analogue filter design which produces the best output response with no ripple in the pass band or the stop band resulting in a maximally flat filter response but at the expense of a relatively wide transition band.

Chebyshev Filter

The Chebyshev filter is popular in RF application - using inductor and capacitor, LC combinations to provide a fast transition from passband to stopband. This transition comes at the cost of in-band ripple, and this may not make it suitable for all applications.

Go to Lesson 7 questions.

Have fun and stay safe.